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Comparison of Crossflow Turbine Performance through Nozzle Position Variations Using ANSYS Simulation

Corvis L Rantererung^{a,*}, Atus Buku^a

^a Mechanical Engineering Department, Paulus Christian University of Indonesia, South Sulawesi, Indonesia Corresponding author: ^{*}corvisrante@yahoo.com

Abstract—The performance comparison of Crossflow turbines is greatly influenced by the position of the nozzle in the conversion of water energy into mechanical energy that occurs through the blades, runners, and shafts of Crossflow turbines. The study aims to directly examine the visualization of water fluid dynamics across the turbine runner blade and enhance the performance of the Crossflow turbine by varying the nozzle position. This study intends to investigate the impact of water flow dynamics and emission on the performance of Crossflow turbines with a combined horizontal-vertical nozzle position, specifically focusing on the magnitude of the number of turbine blades driven and the size of the runner blade area. The objective of investigating nozzle position variations in Crossflow turbines is to determine the specific nozzle position at which the turbine blade may efficiently extract maximum energy from the water flow, hence optimizing turbine performance. The research method using models made using CAD software is AutoCAD by exporting to IGES or IGS format to be compatible with ANSYS. The simulation of this research is with post-processing. There are three, namely making animations, making contours, and taking data to compare cross-turbine performance using variations in nozzle position. Crossflow turbine performance with horizontal nozzle position torque and turbine power is lower, and there is an increase in a vertical position. Then, the horizontal and vertical nozzle position is very good because the nozzle is more effective with maximum turbine performance, namely 13.811-watt turbine power 1,099 turbine torque at 120 rpm.

Keywords-Crossflow turbine; turbine performance; nozzle position variation; ANSYS simulation.

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I. INTRODUCTION

The most famous Crossflow water turbine in rural communities that harnesses the potential water energy as a fundamental energy source available naturally in nature is very environmentally friendly if it can be converted to mechanical forms of energy, electrical energy, and other energy. Improving the quality of life and human civilization is very proper if it uses water energy technically, economically, environmentally friendly, and sustainably [1]-[9]. Water energy in rivers and irrigation canals in rural areas can be used as an energy source to drive micro hydropower plants to serve the community sustainably and economically. The advantages are that the power output is adaptable to conditions and needs, reliable, durable to technology, has low operational costs, and has less environmental impact. Micro hydropower plants can utilize water flow energy freely with a slight discharge, and low head can use Crossflow turbines because of accessible technology, cheap with simple production [3], [10]–[15].

Crossflow turbines have been developed in depth with various methods. The performance of Crossflow turbines is significantly affected by the blade count and the turbine radius ratio[16], [17]. Crossflow turbines are very good to use at low waterfall heights and small water discharge capacities, with straightforward construction, are easy to manufacture, only using local materials and according to the needs in remote areas [11], [18]-[20]. Performance in Crossflow turbines is highly dependent on nozzle position, number of nozzles, geometric shape of turbine blades, fluid flow dynamics, head, water discharge, and energy loss from fluid flow on turbine blades [1], [2], [7], [21]-[28]. The absorption and utilization of water energy through the surface of the water turbine blades is inclined by the dynamic pattern of fluid flow and the concentration of water energy transfer on the surface of the runner blades for mechanical energy conversion as a turbine drive [4]–[6], [9], [29]–[36]. As per the real conditions in the field, Crossflow turbines are already widely used as initial movers in micro hydropower plants in many remote and underdeveloped rural areas[3], [10], [14], [37]-[40].

The most important thing to note in the installation of Crossflow turbine utilization is the emission of inlet water through the nozzle, the component gap between the casing and the runner usually leaks water flow, or there is an excess flow in the penstock pipeline that directs the flow of water into the turbine [21]–[28]. Proper positioning of the turbine blades increases the torque and power of the water turbine as a good main performance. Radial impulse turbines with crossflow turbine types are widely used in various micro hydropower plants in remote areas with small discharges at low water head levels [6], [41], [42]. This Crossflow turbine is very interesting to develop and pursue continuously to improve its performance compared to other water turbines [43]–[46]. It has been popular in the community that Crossflow impulse turbines are straightforward and compact in construction. The main component is two parallel disk circles and a series of turbine blades combined to form a simple turbine runner [47]–[52].

In Crossflow water turbines, there is a dynamic flow of water across the surface of the runner blades with two stages, namely through the first stage, the water jets out of the nozzle and then enters the front edge of the blade to the center of the turbine across the shaft. In the second stage, a jet or jet of water flows from the inside to the outer edge, passing to the next lower blade runner. Then, water radiates from the turbine and is discharged [53]-[55]. The phenomenon of water flowing across the turbine runner twice causes this type of turbine to be given the name Crossflow turbine, and it can convert the kinetic energy of the water jet from the nozzle twice into turbine mechanical energy [49]-[52]. The turbine nozzle is one of the main components of the turbine that functions as a guide and produces water jets to the runner blades of the water turbine [1], [2], [7], [16], [56]. The turbine runner blade component helps receive water beam collisions and then absorb water emission energy from the nozzle when crossing the surface of the water turbine runner blade. Then, the kinetic energy of water absorbed on the surface of the runner blade is passed onto the turbine shaft, which causes rotational motion in the runner [37]–[40], [53]–[55].

The crossflow turbine still has low performance compared to other types of water turbines. So, based on theory, experiment, and practices, information was obtained that the type of Crossflow turbine with a single nozzle at this time, many parts of the turbine blades that the water beam from the turbine nozzle has not touched. Hence, the torque and power of the turbine are still low. The type of Crossflow turbine with a single nozzle in a horizontal position is shown in Figure 1.



1. Air Venting Valve, 2. Distributor, 3. Casing of Turbine, 4. Runner of Turbine, 5. Removable Casing, 6. Blades of Turbine, 7. Flow of Water, 8. Shaft of Turbine

Fig. 1 Water fluid flow model on the Cross turbine [57]

Under the discharge capacity of water entering the turbine blades, crossflow can be calculated [6], [41], [42] using equation (1) as follows:

$$Q = \frac{\sqrt{2.A*g*h}}{t} = V/t(\frac{m^3}{s}) \tag{1}$$

Notes:

A= Nozzle cross-sectional area (m2).

g = Earth's gravitational acceleration constant (m/s2).

h = surface head level height air (m)

V= water volume (m3).

t = time (s).

To find out the waterpower needed by a plant by utilizing water energy is greatly affected by the magnitude of the flow capacity and the height of the waterfall [16], [56], calculated according to equation (2) below:

$$P_{input} = Q * h * \rho * g \qquad (Watt) \qquad (2)$$

The symbol in equation (2) with the description that P_{Input} = input power from water to turbine (Watt), Q = water flow rate (m3/s), h = height of falling water or head (m), ρ = density of water (kg / m3), g = acceleration of gravity (m/s2). The high level or head of water directed into the nozzle converts energy of water pressure into water kinetic, which causes water jets to drive turbine blades and rotate turbine shaft components. The calculation of torque capacity and power generated in Crossflow turbines results from converting water energy absorbed by turbine blades into mechanical energy as the primary mover of the rotating turbine shaft [58], [59]. The calculation follows equation (3) below.

Torque:

$$\tau = F.r \tag{(n.m)}$$

Turbine Power:

$$P_{OutPut} = \tau \varpi \qquad (Watt) \qquad (4)$$

The purpose of the study is to observe the visualization directly of the dynamics of water fluid across the turbine runner blade and improve the Crossflow turbine performance with variations in nozzle position. The magnitude of the number of turbine blades driven or the size of the runner blade area is crossed by the dynamics of water flow emission and its effect on the performance of Crossflow turbines with a combined horizontal-vertical nozzle position. Nozzle position variations in Crossflow turbines also aim to see directly at which nozzle position the turbine blade can absorb as much energy from the water flow beam as possible to improve turbine performance optimally. Crossflow turbines' high and low performance in turbine torque and power is convincingly affected by the pattern or dynamics of fluid flow across the angle that moves the turbine blades that receive and absorb water energy [29], [30], [45], [46], [31]–[36], [43], [44].

II. MATERIALS AND METHOD

The geometry used simulates transient water turbines (changes with time). Because the water turbine that we will simulate rotates around it, we have to make two-fluid models: the rotating area (rotating) and the stationary area (enclosure). Remember that what we are modeling is the fluid of this system, so there is no need to create a solid model. The research model is a simulation using Ansys Software, and in the simulation, the dynamics of water fluid flow flowing across the runner blade of the Crossflow turbine. Crossflow turbines with nozzle position variations are turbines that include dual nozzles, with one positioned horizontally and one positioned vertically, and the option to combine both nozzles in a horizontal-vertical configuration, as illustrated in the schematic model in Fig. 1 as follows:



Fig. 2 Crossflow turbine model scheme with nozzle position variation

The model in Fig. 2 is created in CAD software, such as AutoCAD, by exporting to IGES or IGS format to be compatible with ANSYS.

A. Import Geometry to Ansys

First, open the ANSYS workbench and drag Fluid Flow into the workbench.



Fig. 3 Open ANSYS workbench and drag fluid flow

To quickly import geometry, right-click "geometry" and choose "import geometry." Then, browse and search the existing IGS file.



Fig. 4 Open ANSYS workbench and drag Fluid Flow (Fluent), Select Geometry

The tick on "geometry" indicates that geometry has successfully been imported.

B. Meshing

Double-click on "mesh" to open the meshing window. Click "geometry," then name each part by right-clicking and selecting "create named selection."



Fig. 5 Stage to open the Meshing window

Name it "rotating" for the inner geometry (part 1) and "enclosure" for the outside (part 2). Define inlets and outlets. Select selection to be face selection because we will select surfaces to define. Select the surface to be defined, then "create named selection" to name the surface.



Fig. 6 Stage of "Create named selection" to name the surface

Name it according to the explanation in the geometry figure (topmost) consisting of inlet H, inlet V, and Outlet. After that, define the contact surface between the enclosure and the rotating by first hiding the outermost surface. Click all outermost surfaces (by holding down the Ctrl key), rightclick, and select "Hide face":



Fig. 7 Create a named selection and hide the face

Choose the 'outer' contact surface, i.e., the cylinder around the rotating. "Create named selection" and name it "outer int" (short for outer interface). Then, define the 'inner' contact surface by hiding the enclosure.



Fig. 8 Stage of creating Geometry and hiding body

Once only the rotating part is displayed, click all the outer surfaces to be named "inner int."



Fig. 9 Stage of creating named selection and rotating.

After defining all the parts, the next step is to define the contact between the enclosure and rotating with the settings below:

Project Model (A Project Model (A Project Corr Corr C	3, B3, C3) letry dinate Systems ections Contacts ∑M_ Contact Region d Selections	
Details of "Contact I	Region"	д
Scope		
Scoping Method	Named Selection	
Contact	int luar	
Target	int dalam	
Contact Bodies	Part 2	
Target Bodies	Part 1	

Fig. 10 Stage of defining enclosure contact region and contact bodies

The final step in the meshing process is defining the mesh itself. This case uses mesh with the following settings (explained below):

Sizing		
Use Advanced Size Fun	On: Curvature	
Relevance Center	Medium	
Initial Size Seed	Active Assembly	
Smoothing	Medium	
Transition	Slow	
Span Angle Center	Fine	
Curvature Normal A	Default (18.0 °)	
Min Size	1.e-002 mm	
Max Face Size	5.0 mm	
Max Size	10.0 mm	
Growth Rate	1.10	
Minimum Edge Length	1.09180 mm	
Inflation		
innauon		
Assembly Meshing		

Fig. 11 Stage of Relevance Center

1) Relevance center: The fit of a mesh that is far from a feature. For example, there is a circle hole feature. A mesh with a high relevance center will adjust the mesh away from the circle.

2) Min size, face size, max size: We can determine the maximum and minimum size from the mesh. To set the overall mesh tenuous meeting.

3) Growth rate: The speed of mesh deployment. A high growth rate produces a mesh with an uneven density, while a low growth rate will produce a mesh with an even density.

The above values are primarily determined by the case and the operator's experience. However, the denser the mesh, the more accurate the results will be, and the flow pattern will be smoother. Mesh that is too dense results in computational processes that are too long and even makes solutions divergent (not convergent). Click "Update" to create the mesh. Right-click, then "show all body" and "show all face" to reshow the previously hidden geometry. The meshing process is complete.

C. Computing

Double-click the setup section. Select "parallel," then fill in the number of your processors. In the case of the computer, I use 4 processors, it may be possible to learn the maximum number of cores for other cores. The more processors are used, the faster the computing process, but other software runs slow. Click OK!

Fluent Launcher (Setting Edit Only)	- 🗆 ×
ANSYS	Fluent Launcher
Dimension 2D 3D Display Options Display Mesh After Reading Graphics Windows Workbench Color Scheme Do not show this panel again € Show More Options	Options Double Precision Meshing Mode Use Job Scheduler Use Remote Linux Nodes Processing Options Serial Parallel (Local Machine) Solver Processes 4 0 GPBPUs per Machine None 0
<u>0</u> K	ancel <u>H</u> elp ▼

Fig. 12 Stage of display options, parallel (local machine)

Select the general settings as follows:

Meshing	General
Mesh Generation Solution Setup Solution Setup General Models Materials Phases Cell Zone Conditions Boundary Conditions Mesh Interfaces Dynamic Mesh Reference Values Solution Solution Methods Solution Methods Solution Controls Monitors Solution Initialization Calculation Activities Run Calculation Results Graphics and Animations Plots Reports	Mesh Scale Check Report Quality Display Solver Type Pressure-Based Density-Based Melative Time Gravity Gravity Gravity Gravity Gravity Gravity Gravity Gravity Composition Compositi

Fig. 13 Stage of Select level of general settings

Simulation is transient because there is a spin phenomenon in it. Define gravity in the direction according to the CAD model we created. Use the k-epsilon turbulent model (unless a previous journal already uses another model). The k-epsilon model was chosen because it is a conservative model for various cases and is known for its stability towards convergence.

Meshing	Models	
Mesh Generation	Models	
Solution Setup General Materials Phases Cell Zone Conditions Boundary Conditions Mesh Interfaces Dynamic Mesh Reference Values	Multiphase - Off Energy - Off Viscous - Standard K-e, Standard Wall Fn Radiation - Off Heat Exchanger - Off Species - Off Discrete Phase - Off Solidification & Melting - Off Acoustics - Off Eulerian Wall Film - Off	
Solution Solution Methods Solution Controls Monitors Solution Initialization		
Calculation Activities Run Calculation	< >	•
Results Graphics and Animations Plots	Edit	

Fig. 14 Stage of selecting the general setting: Viscous Standard

Define a new water material by selecting material -> create/edit -> fluent database -> find water liquid.



Fig. 15 Stage of select general setting; water liquid

Define an enclosure as water-liquid:

					-	1 1010							~
Meshing	Cell Zone Co	nditions			Zor	ne Name							
Mesh Generation	Zone				er	ndosure							
Solution Setup	endosure								1	- C			
General	rotating				Mat	terial Name wate	r-liquid	V Edit					
Models						Frame Moti Wate	r-liquid	erms					
Phases						Mesh Motor	Trea roue Trive	orvelues					
Cell Zone Conditions						Forous zone		1			1 1		
Mesh Interfaces					K	tererence Prame	Mesh Motion Porous 2	tone Embe	dded	LES Rea	ction Source Terms P	Fixed Values	Multiphase
Dynamic Mesh Reference Valuer					Г	Rotation-Axis Or	igin		Ro	tation-Axit	s Direction		^
Solution						X (m) 0	constant	~	x	0	constant	~	
Solution Methods Solution Controls						Y (m) 0	constant	~	Y	0	constant	~	
Monitors						76-31							
Calculation Activities	1					2 (m) 0	constant	~	1	1	constant	~	
Run Calculation		Type		ID	_								
Results	mixture	 fluid 	~	6									
Graphics and Animations Plots	Edit	Сору	Profiles		_								
Reports	Parameters	Operating	Conditions										
	Display Mesh	1											
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	Help												
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					-			_	_				
								OK	Can	cel H	elp		

Fig. 16 Stage of select enclosure; water liquid

Define rotating as a rotating area with the following settings:

	101112 m	333			1- Mesh	Tope Name									
ing sh Generation ten Setup dels terials terials terials terials terials terials terials terials terials	Cell Zone Con Zone endosure retating	nditions				rotating Material Nar Frame M Mesh Mo Porous Z Reference	ne water-liqui otion Lami tion LES Ione Frame Mital	d nar Zone Zone 1 Motion	Source ⁻ Fixed Va	Edt ferms ilues Ember] dded LES	Reaction	n] Source Tr	erms Fixed Val	aes Multiphase
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ution Methods ution Controls nitors						Rotation X (m)	-Axis Origin	consta	int	Ŷ	Ro >	tation-Axi	Direction	stant	×
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incs and Animatons	Edit	Copy	Profiles		Wesh (Time=)	Rotation	al Velocity					Translation	nal Velocity		
22	Parameters	Operating	Conditions		Setting in	Speed	(rpm) 120		constant		~	X (m/s)	0	constant	~
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	Help				paral Done. Preparing i Done.										

Fig. 17 Stage of select rotating; water liquid

It should be noted that the rotation axis origin and rotation axis direction must be adjusted to the CAD model that we made at the beginning. Try to make the CAD model we create have a center point in the middle of the rotating circle to make it easier to define the rotation axis origin. If your rotational velocity unit is not in RPM units, you can change it to define-> units. The boundary condition used is the head at the inlet, which is 3.5 m which is converted to pressure form with the equation. $P = \rho$. g. H Choose one (inlet H or inlet V) as inlet pressure and another as the wall.



Fig. 18 Stage of selection either (inlet H or inlet V)

The next step is to define the interface. Since the existing interface cannot be edited directly, we must delete the existing interface first. Then, create a new interface, for example, with the name "int", and define it according to the settings below. One of the crucial things is that we have to change the interface to "matching" to unify the enclosure flow and rotation. Click Create!

Meshing	Mesh Interfaces	1: Mes	ih v	
Mesh Generation olution Setup General Models Materials	Mesh Interfaces	=		~ ~
Cel Zone Conditions		Create/Edit Mesh Interfaces		×
Mesh Interfaces		Mesh Interface	Interface Zone 1	Interface Zone 2
Dynamic Mesh Reference Values		Int	Int_uar-contact_region-src	Int_dalam-contact_region-org
olution		10 m	= 2	
Solution Methods Solution Controls Monitors Solution Initialization			int_dam-contact_region-src	int_dalam-contact_region-erg
Calculation Activities Run Calculation	Create/Edit	Interface Options	Boundary Zone 1	Interface Wall Zone 1
esults Graphics and Animations Plots	Preview Mesh Motion	Periodic Boundary Condition Periodic Repeats Coupled Wall	Boundary Zone 2	Interface Wall Zone 2
Reports	Help	Matching		Interfare Interior Zone
				interior-16
		Periodic Boundary Condition Type Offset Relational Auto Compute Offset	Y (n) 0 Z (n) este Delte Draw List C Ling Post Processing and Sur	0 Joze Help Faces Information Done.

Fig. 19 Stage of select mesh interface.

The solution method, control, and monitors are not discussed in detail because they depend on operator experience and trial and error. Use the existing defaults if you are confused to edit them. Initialize each time you start a new simulation. Use a hybrid or standard initialization from one of the inlets we analyze. In calculation activities, setting "autosave every" with a low value will result in animations with smoother movements but will take up much memory and slow down the whole process. In this simulation, we use autosave every 1-time step to create animations and 5 for cases where torque data is needed only (no animation needed). Use the run calculation settings below:



Fig. 20 Stage of Run Calculation

1) Time steps: This is the unit of time in seconds for each iteration. Like an animation, the smaller the time steps, the

smoother the movement. However, if it is too small, it will take a considerable number of steps (Number of time steps) to analyze at a specific time. The time analysis can be calculated by multiplying the time and number of time steps. Suppose Time steps = 0.01s, and the number of time steps = 200. Then, the time covered in the simulation is 0.01*200 = 2 seconds.

2) Autosave Every: This value is the number of time steps when the frame is saved for later display in the animation. Suppose we input the value 5 in Autosave Every, while, we have a value of 0.01 s in time steps. Then, the image appearing in the animation is every 0.01*5 = 0.05 second in the simulation. That is, if the simulation includes a simulation time of 2 seconds, then the total number of animation frames is 2/0.05 = 40 frames (or images) to form the entire animation.

3) Max iteration/time step: The number of iterations each time step. Suppose we enter the value 3 in this parameter and 200 in the number of time steps. Then, the total iteration of this simulation is 300 times. The more Max iteration/time steps values, the more accurate the results, but the number of total iterations will be huge. Click Calculate to start the simulation and wait patiently. For new input, you only need to change the rpm value and reinitialize to reset the data and re-simulate with the new data.

D. Post Processing

The purpose of post-processing is threefold: making animations, making contours, and retrieving data.

1) Data retrieval process: Data taken from turbine simulations in torque and drag. Torque calculation can be calculated using the Calculators -> Function: Torque, Location: Blade, Axis: Global X. Calculate feature!

Outline	e Variabl	es Expre	essions	Calcula	tors	4 🕨	
M	Macro Ca	lculator					
	Mesh Cal	culator					
<u>^</u>	Function	Calculator					
Fund	ction Calcu	lator					
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Loc	ation	blade			-		
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-46	.7385 [N m]						
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Fig. 21 Stage of Run Post-Processing

Remember that this simulation is transient; it changes with time. Therefore, the torque and drag values will change every second. To adjust the "position" of the time or angle of rotation, you can click on the "Time step selector". Double-click on the "time" you want.

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	6	40	40	0.2	Full	_	
	7	45	45	0.0	Full		
	á	50	50	1	Full		
	Ğ	55	55	11	Full		
	10	60	60	1 2	Full		
-	11	65	65	13	Full		
	12	70	70	1.4	Full		
Case-	13	75	75	1.5	Full		
1	14	80	80	1.6	Full		
- 11	15	85	85	1.7	Full		
	16	90	90	1.8	Full		
	17	95	95	1.9	Full		
	18	100	100	2	Full		
	19	105	105	2.1	Full		
	20	110	110	2.2	Full		
	21	115	115	2.3	Full		
	22	120	120	2.4	Full		
	23	125	125	2.5	Full		
	24	130	130	2.6	Full		¥

Fig. 22 The stage of sets the "position" of the time or angle of rotation, can be clicked on the "Time step selector"

2) Creating a contour plot: To create a contour plot, we first define the location where the plot is drawn by selecting the location -> plane menu. Select the plane's location as needed. Contours can be created by directly clicking on the shortcut "Contour". Use the settings below:

😤 🕰 🛃 🗿 🦻 🥲 🔞 Location 🗸 🕏 📶
Outline Variables Expressions Calculators (
 rotating it blade it_int_dalam contact_region trg
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Details of Contour 1
Geometry Labels Render View
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Locations Plane 1
Variable Velocity 🗸
Range User Specified 👻
Min 0.0 [m s^-1]
Max 4.6 [m s^-1]
Boundary Data O Hybrid O Conservative
Color Scale Linear -
Color Map Default (Rainbow) 👻 📄
of Contours 80

Fig. 23 Creating a contour plot

Choose a variable according to your needs, for example, velocity or pressure. The range -> user specified is used to maintain the consistency of simulation results. If the image is not intended to be simulated, it is recommended to use "local". # of higher contours will make the contour smoother, but too high a value can slow the extraction process in animation creation.

3) Creating Animations: Animation creation is done by returning to the shortcut "Timestep Selector", then selecting the block of all "time" and selecting the shortcut "Animate Timestep."

🕑 Ti	mestep	Selector			?
FFF					
Loade	d Times	step: 35			
#	Step	Solver Step	Time [s]	Туре	^
28	150	150	3	Full	
29	155	155	3.1	Full	
30	160	160	3.2	Full	
31	165	165	3.3	Full	
32	170	170	3.4	Full	- 11
33	1/5	1/5	3.5	Full	
34	180	180	3.0	Full	
22	100	100	3.7	Full	
27	105	105	2.0	Full	
29	200	200	4	Full	
39	205	205	4 1	Full	
40	210	210	4.2	Full	
41	215	215	4.3	Full	
42	220	220	4.4	Full	
43	225	225	4.5	Full	
44	230	230	4.6	Full	
45	235	235	4.7	Full	
46	240	240	4.8	Full	
47	245	245	4.9	Full	
48	250	250	5	Full	
49	255	255	5.1	Full	
50	260	260	5.2	Eull - Final	

Fig. 24 Animation creation

Check "Save movie" and select the folder where you want to save the animation, then click the play icon to run the animation and save the animation.

Animation		
O Quick Anin	ation	
Timestep /	Animation	
○ Keyframe	Animation	
	1.00	
		Current Timestep: 55
Control By	Timestep	•
Specify Ra	nge for Animation	Ξ
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		v
Repeat	1	* C0
Save Mo	vie C:/Users/Caesar Wiratama/Documents/FFF.wmv	Ĕ
Format	Windows Media Video	•
		Options

Fig. 25 Run animations while saving animations

III. RESULTS AND DISCUSSION

A. Simulating Crossflow Turbine Performance with Nozzle Position Variation

1) Simulating Crossflow Turbine Performance with Nozzle Position Variation: Based on the torque data

calculated from post-processing above, these data are compiled in Microsoft Excel by comparing them to rpm, and power can be calculated and tabled in Table 1.

2) Animation of fluid dynamics in Crossflow turbine with horizontal nozzle position: In Table 1, Figs. 26 and 27

illustrate Crossflow turbine performance with a horizontal nozzle position illustrating the spray of incoming water on the turbine runner blades. The animation of fluid flow dynamics is visible, which illustrates that in a Crossflow turbine with a horizontal nozzle, as shown in Fig. 28.

TABLE I
TURBINE CROSSFLOW PERFORMANCE SIMULATION RESULTS WITH NOZZLE POSITION VARIATIONS

No —	Lap	Horizontal Nozzle Position		Nozzle Vertical Position		Horizontal and Vertical Nozzle Combined Position	
	rpm	Torque (nm)	Power (Watt)	Torque (nm)	Power (Watt)	Torque (nm)	Power (Watt)
1	120	0.806814	10.138723	0.915803	11.508319	1.0991	13.811697
2	140	0.542649	7.955649	0.627754	9.203354	0.7314	10.724335
3	150	0.461252	7.245329	0.527938	8.764069	0.6103	9.586962
4	160	0.363370	6.088322	0.408153	6.838669	0.5073	8.501065



Fig. 26 Graph Turbin Torque Vs Turbine Speed



Fig. 27 Graph Turbine Power vs. Turbine Speed



Fig. 28 Cross Flow Turbine Animation with Horizontal Position

Based on the animation results, the flow of water fluid is more stable through the runner blade chamber of the turbine. The horizontal crossflow nozzle radiates water to pound the driven turbine blades [3], [8]. The animation movement of water jets across the runner blade begins as a fluid flow moves the two-stage blade. According to the results of direct observations, the fluid dynamics generated by the horizontal nozzle propel the runner blade of the water turbine, allowing it to harness the energy of the water efficiently in a single stage [1], [2], [4]-[7], [9]. The optimal turbine power produced is lower in a Crossflow turbine using a horizontal nozzle position, which is 10.138 Watts, with a torque of 0.806 nm (Joule) because of fluid flow dynamics. The animation demonstrates the flow of the working fluid in a Crossflow turbine with a horizontally positioned nozzle. It illustrates that the working fluid, when emitted from the nozzle, imparts motion to the blades of the Crossflow turbine. Before reaching the blade chamber in the 2nd stage turbine, it results in the loss of hydraulic energy of the water jet and the change of water jet direction when entering the blade chamber of the second stage turbine, and conditions such as this significantly affect the reduction in turbine performance [3], [10], [14].

3) Fluid animation on crossflow turbine with vertical nozzle position: Table 1 and Figs. 26 27 above show the Crossflow turbine performance with a vertical nozzle position using a Crossflow turbine after operating or running stably and then visually observed the animation of the fluid flow Crossflow turbine with cross flow power with a nozzle position vertical began to increase by 11, 508 watts with a torque of 0.915 nm (Joule). The animated graphic demonstrates how a Crossflow turbine with a vertical nozzle emits and directs water into the turbine. Additionally, the animation showcases the fluid movement of water on a Crossflow turbine with a vertically positioned nozzle. Upon observing the animation image, it becomes evident that the animation of the fluid flow in the vertical nozzle crossflow turbine exhibits vertical radiation only. The water jet passes through the turbine blades in a crossflow configuration, exerting force on the blades in a single stage, allowing the blades to exclusively harness the energy from the water. The water jet entering the turbine solely impacts the blades, which causes the turbine performance with a vertical nozzle position to increase further, and the animated image can be seen in Fig. 29 as follows.



Fig. 29 Crossflow turbine animation with vertical position

4) Animation of fluid flow on crossflow turbine with combined Horizontal and vertical nozzle positions: The data from the research simulation described in Table 1 and Figs 26 and 27 above shows the crossflow turbine performance with a combination of horizontal and vertical nozzle positions is to receive water jets into the turbine from two stages, namely from the horizontal and vertical sides, this is so that more blades are crossed by water spray from the nozzle [11]–[13], [15]. The firsthand measurements unequivocally demonstrate the fluid flow dynamics that water jets generated, which originate from the nozzle. The drive for water turbine blades is achieved by a Crossflow pattern [17], [60]. The water beam emitted from the horizontal nozzle is guided by the water beam emitted from the vertical nozzle, resulting in enhanced absorption of water energy by the turbine blades leading to the increase of turbine's power and efficiency.

According to the animation pattern of fluid dynamics associated with the performance of the turbine cross nozzle, the combined horizontal-vertical nozzle position is substantial. Crossflow turbines have superior fluid flow dynamics, efficiently converting water energy into rotational motion by directing it onto the surface of the turbine blades. The graph in Fig. 9 clearly illustrates the positive correlation between turbine power and variations in water discharge. It is evident that when the flow rate increases, the turbine power also rises, highlighting the most significant difference [37]-[40]. The performance of Crossflow turbines with vertical horizontal combined nozzles has increased significantly, and the highest is 13,811-watt turbine power at 1,099 nm (Joule) of torque with 120 rpm rotation. Crossflow turbines with combined nozzles can produce greater turbine power and torque due to a more precise and effective fluid flow dynamics pattern in the direction of water jetting into the turbine runner blades [6], [41], [42]. The turbine runner absorbs more outstanding water energy blades to produce greater turbine shaft power, as illustrated in the animation in Fig. 30.

The fluid dynamics of the Crossflow turbine blades have a highly favorable impact on enhancing the performance of the turbine when equipped with the Horizontal-Vertical Combined Nozzle Position. It is essential to carefully evaluate the interaction between the turbine blade and the water jet that is released from the turbine nozzle. This can be achieved by adjusting the design of the turbine blade to align with the flow that enters the blade area. The animation depicts the fluid flow dynamics that result in low turbine performance at low discharge. This occurs because the flow dynamics have sufficient time to fill the imperfections in the turbine blades and flow in a crossflow manner [11]–[13], [15].



Fig. 30 Crossflow turbine animation with combined horizontal-vertical nozzle position

Nevertheless, when the velocity of the working fluid discharged from the nozzle is high, it prevents the working fluid from recirculating within the turbine blades. There is no crossflow movement from the uppermost blade level to the lower second blade level. By directly observing the image of the fluid flow pattern created by the water jet from the nozzle, it is evident that the fluid flow can reach multiple blades, resulting in the rotation of the water turbine. This rotation increases turbine power and torque, making it more efficient [11], [17]–[20], [60]. This shows that the more the speed of fluid flow increases, the more the inflow of turbine blades will tend to be turbulent. In Crossflow turbines using the horizontal nozzle position, the optimum turbine power produced is lower at 10.138 Watts, with a torque of 0.806 nm (Joule) because the water beam from the nozzle does not occur transverse flow. The turbine blade undergoes a single step of energy absorption, with only a limited number of blades propelled by water jets. The power output of the crossflow turbine rose by 11,508 Watts, and the torque increased by 0.915 nm (Joules) when the vertical nozzle position was adjusted. The Crossflow turbine exhibits a nozzle that is both vertical and horizontal in orientation. This design results in a substantial and maximum increase in turbine power, specifically 13,811 Watts at a torque of 1,099 nm (Joule) and a rotation speed of 120 RPM.

The velocity of lateral water flow, known as crossflow, significantly impacts the turbine's runner blades, leading to increased torque and power output. In a Crossflow turbine employing a combination of nozzle locations, the water jet emanating from the nozzle exerts a greater and more uniform force on the turbine blades, resulting in a twofold increase in the absorption of water energy by the blades. The crossflow turbine simulation results employ a configuration where the nozzle is positioned both horizontally and vertically. This arrangement allows the turbine blades to capture significant energy from the water flow efficiently, enhancing the turbine's power output and maximum torque [53]–[55]. The combined Crossflow nozzle turbine is a turbine that operates twice. The efficient conversion and transfer of kinetic energy from water onto the turbine runner blade is effectively utilized to maximize the utilization of water energy sources as the primary driving force for a future power plant [53]–[55].

IV. CONCLUSION

The simulation settings we make produce power values in an order that approximates the results of experiments and simulations according to intuition. Then, based on the graph of power to rpm, a graph shows a trend of decreasing power to increasing rpm. Based on the graph of power to RPM, the overall performance at all rpm values, from highest to lowest, is combined inlet, vertical, and horizontal. The results of simulation and animation of fluid flow dynamics in a Crossflow turbine with a horizontal and vertical combined nozzle position preserve performance improvement due to water beam from the nozzle is able to cross the turbine runner and crossflow, more blades, drive the two-stage turbine runner blades, drive the turbine blades twice as many blades on the turbine runner. Achieve maximum turbine performance with a power of 13,811 Watts at a turbine torque of 1,099 with a rotation of 120 RPM. Crossflow turbines that use only horizontal or vertical nozzle positions show lower power performance, producing turbine torque.

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